



32 **Abstract**

33 The hidden Markov model (HMM)-based approach for eye movement analysis is able to  
34 reflect individual differences in both spatial and temporal aspects of eye movements.  
35 Here we used this approach to understand the relationship between eye movements  
36 during face learning and recognition, and its association with recognition performance.  
37 We discovered holistic (i.e., mainly looking at the face center) and analytic (i.e.,  
38 specifically looking at the two eyes in addition to the face center) patterns during both  
39 learning and recognition. Although for both learning and recognition, participants who  
40 adopted analytic patterns had better recognition performance than those with holistic  
41 patterns, a significant positive correlation between the likelihood of participants' patterns  
42 being classified as analytic and their recognition performance was only observed during  
43 recognition. Significantly more participants adopted holistic patterns during learning than  
44 recognition. Interestingly, about 40% of the participants used different patterns between  
45 learning and recognition, and among them 90% switched their patterns from holistic at  
46 learning to analytic at recognition. In contrast to the scan path theory, which posits that  
47 eye movements during learning have to be recapitulated during recognition for the  
48 recognition to be successful, participants who used the same or different patterns during  
49 learning and recognition did not differ in recognition performance. The similarity  
50 between their learning and recognition eye movement patterns also did not correlate with  
51 their recognition performance. These findings suggested that perceptuomotor memory  
52 elicited by eye movement patterns during learning does not play an important role in  
53 recognition. In contrast, the retrieval of diagnostic information for recognition, such as  
54 the eyes for face recognition, is a better predictor for recognition performance.

55

56 Keywords: individual difference, eye movement, hidden Markov model, face learning,  
57 face recognition

58

59 **Introduction**

60 In human vision, the density of photoreceptors on the retina is not uniform. It is  
61 extremely high at the fovea, and drops dramatically as visual eccentricity increases. Thus,  
62 the fovea has the highest visual acuity, whereas the perifoveal area, which is much larger  
63 than the fovea, is of low visual acuity. In order for an individual to see clearly a region of  
64 interest in a cognitive task, the fovea has to be constantly relocated to the region (Tovee,  
65 1996). Consequently, our eyes are constantly moving, and eye movements are shown to  
66 reflect underlying cognitive processes, or more specifically the way information is  
67 sampled from the environment (Antrobus, Antrobus, & Singer, 1964; Yarbus, 1967; Grant  
68 & Spivey, 2003; Heremans, Helsen, & Feys, 2008). Thus, it is reasonable to speculate that  
69 different eye movement patterns may lead to different performances in cognitive tasks.

70 Consistent with this speculation, it has been reported that in a cognitive task, experts  
71 and novices typically exhibited different eye movement patterns. For instance, Charness  
72 et al. (2001) reported that expert and intermediate chess players have different eye  
73 movement patterns. Experts made significantly more fixations at empty squares on the  
74 board. They also fixated significantly more often at pieces relevant to the current task  
75 than did the intermediates. Waters and Underwood (1998) compared the eye movement  
76 patterns of expert and novice musicians when they participated in a simple music reading  
77 task. The participants were shown two melodic fragments successively, and asked to  
78 judge whether the two fragments were the same or different. It was found that experts  
79 made significantly more fixations at the first fragment than novices and that their initial  
80 fixations were of significantly shorter duration than the novices. Similar findings were  
81 also reported in the research on reading. Siyanova-Chanturia, Conklin, and Schmitt (2011)  
82 compared the eye movement patterns of native and non-native English speakers when  
83 they were asked to read idioms and novel phrases. It was found that native speakers made  
84 significantly fewer and shorter fixations at idioms than novel phrases. In contrast, the  
85 number and duration of fixations that non-native speakers made at idioms and novel  
86 phrases were similar to each other. This demonstrated that native speakers had a  
87 processing advantage for idioms over novel phrases, which was not presented among  
88 non-native speakers. Hyona, Lorch, & Kaakinen (2002) compared eye movement patterns  
89 of native Finnish speakers when they were reading Finnish texts and found that those

90 who fixated more often at the headings and topic-final sentences performed significantly  
91 better than those who showed other eye movement patterns when they were required to  
92 summarize the texts.

93         Nevertheless, in the literature on face recognition, it remains controversial whether  
94 different eye movement patterns are associated with different recognition performances.  
95 For example, Goldinger, He, and Papesh (2009) found that in a face recognition memory  
96 task, participants made fewer fixations, visited fewer regions of interest, and had shorter  
97 scanning distances on the trials in which they failed to recognize a learned face as  
98 compared with those that led to successful recognition. Glen et al. (2012) found that  
99 among people who suffered from central visual field defects, those who performed better  
100 in face recognition demonstrated a different eye movement strategy as compared with the  
101 ones who performed worse. These findings suggest that eye movement patterns are  
102 associated with performance in face recognition. In contrast, Blais et al. (2008) found that  
103 in face recognition, although Asian participants looked primarily at the center of the faces  
104 (i.e., a holistic scanning pattern) whereas Caucasian participants looked more frequently  
105 at facial features such as the two eyes and the mouth (i.e., an analytic pattern), the two  
106 cultural groups showed comparable recognition performance. This finding was later  
107 replicated in Caldara, Zhou, and Miellat (2010). Similarly, Mehoudar, Arizpe, Baker, &  
108 Yovel (2014) found that participants showed idiosyncratic eye movement patterns in face  
109 recognition that were highly stable over time; however, these patterns were not predictive  
110 of their recognition performance.

111         These inconsistent findings in the literature may be due to substantial individual  
112 differences in eye movement pattern that were not adequately reflected in the data  
113 analyses. Indeed, recent studies have shown that there are considerable individual  
114 differences in eye movement that persist over time and across different stimuli when  
115 people perform cognitive tasks. For instance, Castelhana and Henderson (2008) showed  
116 that during picture viewing, the characteristics of fixation durations and saccade  
117 amplitudes in eye movement differed across individuals but were stable within an  
118 individual across different types of visual stimuli. Risko et al. (2012) found that curiosity  
119 was a significant predictor of participants' eye movement patterns in scene viewing.  
120 Peterson and Eckstein (2013) showed that participants differed significantly in where to

121 first move their eyes in a face identification task, and they performed better when being  
122 forced to look at their preferred viewing locations than other locations. Kanan, Bseiso,  
123 Ray, Hsiao, and Cottrell (2015) showed that the identity of participants could be inferred  
124 based on their eye movements across different face perception judgment tasks. These  
125 findings provided stronger evidence for the existence of substantial individual differences  
126 in eye movement.

127 In order to account for individual differences in both spatial (i.e., fixation locations)  
128 and temporal dimensions (i.e., transitions among fixation locations) of eye movement in  
129 the data analysis, in our previous study (Chuk, Chan, & Hsiao, 2014a), we proposed to  
130 use a hidden Markov model (HMM) to summarize an individual's eye movement pattern  
131 in face recognition. The hidden states of the HMM represented the individual's regions of  
132 interests (ROIs) for eye fixations. The individual's eye movements among the ROIs were  
133 summarized through the HMM's transition matrix, which represents the probability of  
134 each ROI being viewed next conditioned on the currently viewed ROI. The process of  
135 learning the individual HMMs was completely data driven. The individual HMMs could  
136 then be clustered based on their similarities to discover common patterns shared by  
137 individuals. The similarity of an individual pattern to a common pattern discovered  
138 through clustering could be measured as the likelihood of the individual pattern being  
139 classified as the common pattern. Through this approach, we discovered two common  
140 eye movement patterns in face recognition within our Asian participants that resembled  
141 the holistic and analytic patterns found in Asian and Caucasian participants respectively  
142 in Blais et al. (2008) and Caldara et al. (2010). This finding showed that both eye  
143 movement patterns could be observed within a cultural group, demonstrating substantial  
144 individual differences in eye movement pattern. In our follow-up study (Chuk et al.,  
145 2014b; Chuk, Crookes, Hayward, Chan, & Hsiao, submitted), we found that analytic and  
146 holistic patterns could be observed in both Asians and Caucasians, and the two cultural  
147 groups did not differ significantly in the percentage of group members being classified as  
148 using holistic or analytic patterns. Also, the participants who showed analytic eye  
149 movement patterns performed significantly better than those who showed holistic  
150 patterns, and there was a positive correlation between the likelihood of participants'  
151 pattern being classified as analytic and their recognition performance. These findings

152 were not possible without taking individual differences in eye movement into account,  
153 demonstrating well the advantage of our HMM approach.

154 Our results from previous studies suggested that analytic eye movement patterns,  
155 which involved eye fixations specifically to the two eyes in addition to the face center,  
156 were beneficial for face recognition. This result was consistent with the previous studies  
157 showing that the eyes are the most important features for face recognition (e.g., Gosselin  
158 & Schyns, 2001; Vinette, Gosselin, & Schyns, 2004). For example, using the Bubbles  
159 technique, Gosselin and Schyns (2001) found that the two eyes were the most diagnostic  
160 features for recognizing the identity of an individual. Vinette et al. (2004) further showed  
161 that the left eye was the earliest diagnostic feature that participants used in face  
162 recognition. Afterwards, both the left and right eyes were used effectively.

163 Nevertheless, it remains unclear whether analytic eye movement patterns are also  
164 beneficial for face learning. Henderson, William, and Falk (2005) found that when  
165 participants' eye movements were restricted to be at the face center during the learning  
166 phase of a face recognition task, their performance in the recognition phase was impaired  
167 significantly. This result suggested that the eye movements during the learning phase  
168 were related to recognition performance. Sekiguchi (2011) further showed that  
169 participants who had high face recognition memory performance moved their eyes  
170 between the left and right eyes more frequently (i.e., an analytic eye movement pattern)  
171 during face learning than those with low recognition performance. This result suggests  
172 that, similar to eye movements during face recognition, analytic eye movement patterns  
173 during face learning may also be associated with better recognition performance.

174 In addition, in the literature, it has been suggested that during visual recognition,  
175 participants showed similar eye movements to those generated during visual learning. For  
176 instance, the scan path theory posits that in pattern perception, the mental representation  
177 of visual patterns includes the perceptuomotor cycle involved during memory encoding.  
178 Accordingly, eye movements produced during learning have to be repeated during  
179 recognition for the recognition to be successful (Noton & Stark, 1971a; 1971b).  
180 Consistent with this theory, Laeng and Teodorescu (2002) found that when participants  
181 were asked to recall a learned picture in front of a whiteboard, they had better  
182 performance when their eyes were allowed to move freely than restricted to be at the

183 center of the board, and their eye movements resembled those generated during learning.  
184 In face recognition, Blais et al. (2008) found that although in general, participants in the  
185 recognition phase made fewer fixations than in the learning phase, their eye movements  
186 did not show any significant difference in terms of fixation location or duration during  
187 the two phases. More specifically, Asian participants consistently showed holistic eye  
188 movement patterns whereas Caucasian participants showed analytic patterns in both the  
189 learning and recognition phases (see also Caldara et al., 2010). In contrast, some studies  
190 have shown that an exact repetition of eye movements during learning was not necessary  
191 for successful recognition. For example, participants were able to recognize previously  
192 learned visual stimuli in tachistoscopic presentations, in which eye movements were not  
193 possible (e.g., Thorpe, Fize, & Marlot, 1996). They were also able to recognize faces  
194 when their eye gaze was restricted to be at the face center during learning, and their eye  
195 movements during recognition were similar to those generated when they were allowed  
196 to move their eyes freely during learning (Henderson et al., 2005). However, these results  
197 did not completely rule out the influence of perceptuomotor memory in pattern  
198 recognition as suggested in the scan path theory. It remains possible that participants who  
199 show more similar eye movement patterns during face learning and recognition perform  
200 better in face recognition than those who show different patterns.

201 Indeed, eye movements during pattern recognition can be influenced by multiple  
202 factors in addition to perceptuomotor memory, such as top-down expectations and  
203 bottom-up image saliency, and thus eye movement patterns during recognition may not  
204 be exact replications of those generated during learning (e.g., Henderson, 2003; Rayner,  
205 1998; Yarbus, 1965). Accordingly, eye movements during learning and recognition  
206 should differ because the two phases involve different task expectations and cognitive  
207 processes: information encoding during learning, and information retrieval during  
208 recognition. Consistent with this speculation, Hsiao and Cottrell (2008) found that during  
209 face learning and recognition participants showed different fixation duration profiles:  
210 during face learning, participants' first fixations were short, and the duration gradually  
211 increased for the second and then the third fixations, whereas during recognition, there  
212 was no difference between the first three fixations in terms of duration. Nevertheless, in  
213 contrast to this finding, Blais et al. (2008) reported that participants' eye movement

214 patterns during face learning and recognition did not differ significantly in either fixation  
215 location or duration (see also Caldara, et al., 2010). We speculate that this inconsistency  
216 may be because participants differed in whether they used similar eye movement  
217 strategies for face learning and recognition, and this individual difference might have  
218 been obscured in group-level analysis used in previous studies. In addition, this  
219 individual difference may also be related to their recognition performance, as suggested  
220 by the scan path theory. Such examination requires individual-level eye movement  
221 pattern analysis.

222 Thus, here we aimed to examine whether participants used different eye movement  
223 patterns for face learning and recognition through individual-level data analysis using the  
224 HMM based approach. We also aimed to examine whether eye movement patterns during  
225 face learning were associated with performance during the recognition phase, and  
226 whether the similarities between participants' eye movement patterns during face learning  
227 and recognition were related to their recognition performance. In view of the previous  
228 finding that eye movements in face learning and recognition may differ in fixation  
229 duration (Hsiao & Cottrell, 2008), in the current study we included fixation duration  
230 information in addition to fixation location information in the HMMs. This expansion of  
231 the model allowed us to model participants' eye movement patterns more precisely. We  
232 hypothesized that: 1) During face learning, common eye movement patterns similar to the  
233 holistic and analytic patterns discovered during face recognition may also be observed,  
234 and participants with analytic patterns during face learning may also perform better in  
235 face recognition than those with holistic patterns; 2) Participants may use different eye  
236 movement patterns during face learning and recognition, reflecting different underlying  
237 cognitive processes; 3) Individuals differ in the similarity between eye movement  
238 patterns during face learning and recognition, and this similarity may be associated with  
239 their recognition performance, as suggested by the scan path theory.

240

241

## 242 **Method**

### 243 **Behavioral task**

244



245 Here we used the data collected in Chuk, Crookes, Hayward, Chan, and Hsiao (submitted;  
246 see also Chuk et al., 2014b) for the data analysis. A total of 48 participants (24 Asians and  
247 24 Caucasians) were recruited for a face recognition task. The mean age of Asian  
248 participants (7 males) was 21.5 (SD = 2.2), whereas that of Caucasian participants (6  
249 males) was 21.2 (SD = 7.5). The task had two sessions, one with Asian face images and  
250 the other with Caucasian face images (counterbalanced across participants). Each session  
251 had a learning phase and a recognition phase. There was no time delay between the two  
252 phases, but participants were allowed to take a break between the two sessions.  
253 Participants in each learning phase were required to view 14 faces one at a time, each for  
254 5 seconds. In each recognition phase, they were presented with the 14 learned faces and  
255 14 new faces one at a time, and were required to judge through button responses whether  
256 they saw the face during the learning phase or not; the face image stayed on the screen  
257 until the response. During both phases, participants started each trial with a central  
258 fixation cross. The face image was then presented at one of the four quarters on the  
259 screen in a random order. The distance between the central fixation cross and the image  
260 locations subtended about 9 degrees of visual angle horizontally and about 7 degrees  
261 vertically. The face images subtended about 8 degrees of visual angle horizontally and 13  
262 degrees vertically. Participants' eye movements were recorded with an EyeLink 1000 eye  
263 tracker.

264 Eye movement data were extracted from the EyeLink 1000 system using the  
265 default software Data Viewer. In data acquisition, the EyeLink 1000 defaults for  
266 cognitive research was used: saccade motion threshold was 0.15 degree of visual angle;  
267 saccade acceleration threshold was 8000 degree / square second; saccade velocity  
268 threshold was 30 degree / second. The software produced a fixation report for each  
269 participant. We then filtered out fixations that were not located in the face area. The  
270 remaining eye movement data were used for data analyses.

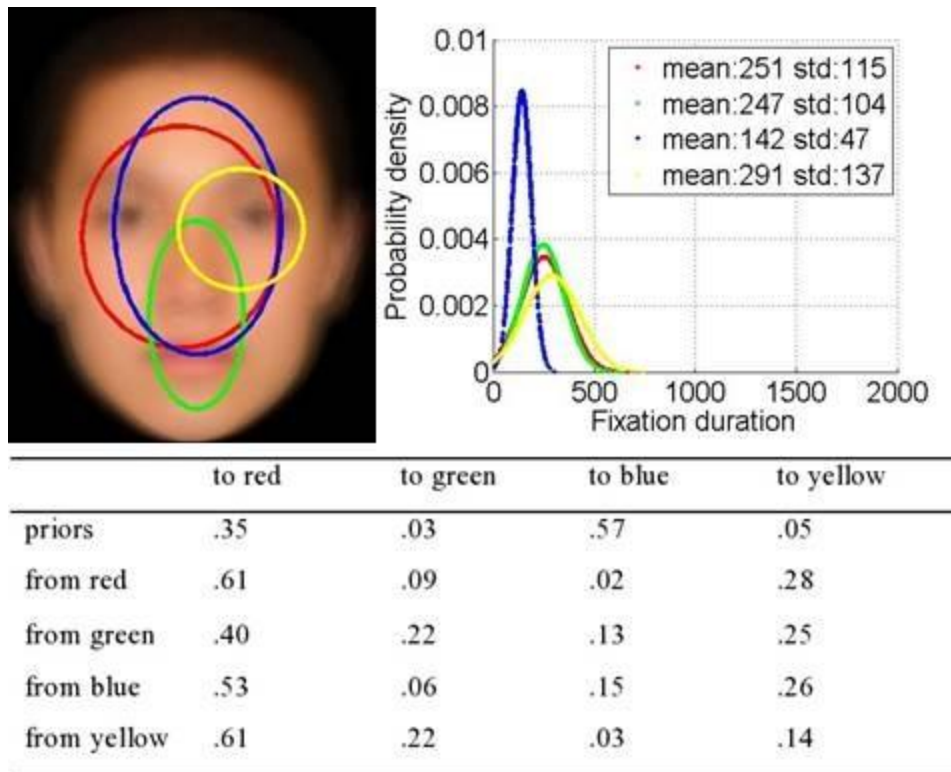
### 271 **Hidden Markov models**

272 We assumed that a participant's eye movements in a cognitive task could be summarized  
273 with a hidden Markov model (HMM), so that we were able to examine individual  
274 differences in eye movements through comparing individual HMMs. Furthermore, we  
275 clustered the individual HMMs to discover common patterns (the toolbox, Eye movement

276 hidden Markov models approach (EMHMM), can be downloaded here:  
277 <http://visal.cs.cityu.edu.hk/research/emhmm/>).

278 HMMs are a type of time-series model that assumes that the observed time-series  
279 data arise from an underlying state process, where the current state depends only on the  
280 previous state. The underlying states are hidden; they can be estimated from the  
281 probabilistic association between the observed data and the states (i.e., the emission  
282 density of a state), as well as from the transition probabilities between the states. An  
283 HMM contains a vector of prior values, which indicates the probability of a time-series  
284 beginning with each state; a transition matrix, which specifies the transition probabilities  
285 between any two hidden states; and a Gaussian emission for each state, which represents  
286 the probabilistic association between the observed data (e.g., eye fixation locations) and a  
287 hidden state.

288 In the context of eye movement analysis here, the observed time series were eye  
289 fixation sequences, with each observation consisting of both fixation location and fixation  
290 duration. Each hidden state of the HMM represented a Region of Interest with Duration  
291 (ROID), which contained the location of the region of interest (ROI), as well as fixation  
292 duration in the ROI (Note that in our earlier implementation reported in Chuk et al., 2014,  
293 we did not include duration information). We assumed that both the locations and  
294 durations of the fixations belonging to an ROID followed a Gaussian distribution (see  
295 Ohl, Brandt, & Kliegl, 2013). Each ROID therefore was represented as a three-  
296 dimensional Gaussian emission, where two dimensions corresponded to the spatial  
297 distributions of the fixations (i.e., fixation locations), and the third dimension  
298 corresponded to the temporal distribution of the fixations (i.e., fixation durations). In the  
299 HMM, the prior vector indicated the probabilities that a fixation sequence started in a  
300 particular ROID, while the transition matrix contained the probabilities of moving to the  
301 next ROID from the current ROID. Figure 1 shows an example HMM. An acyclic graph  
302 whose nodes represent the components of the HMM is shown in Figure 2.



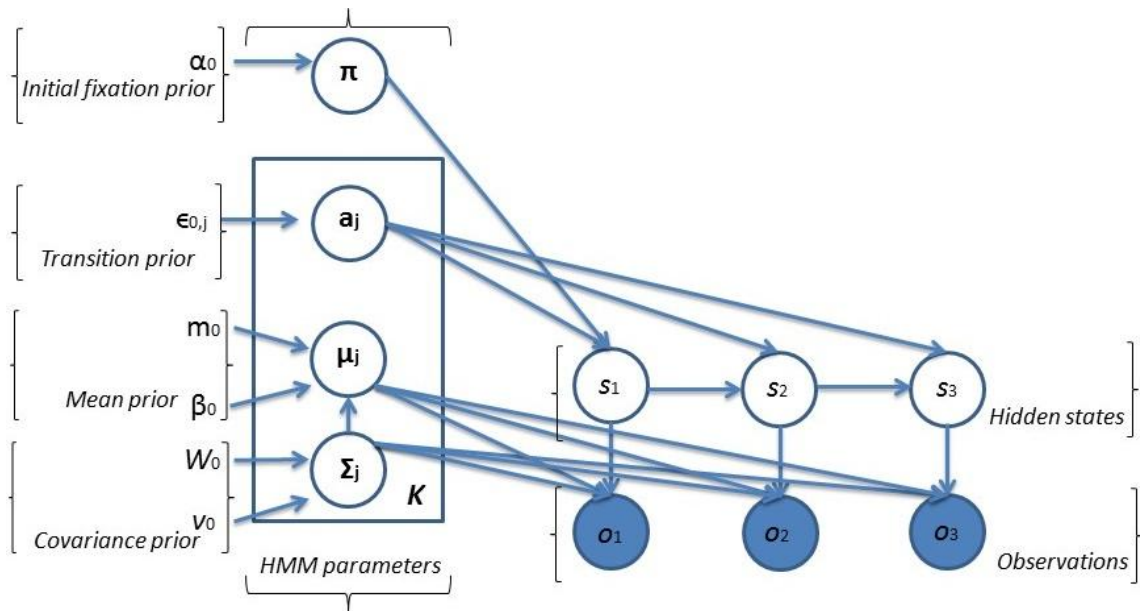
303

304 Figure 1. An example of an HMM summarizing eye fixation data. The ellipses on the face  
 305 represent the location of the ROIDs. The ellipse represents 2 standard deviations around  
 306 the mean of the Gaussian spatial distribution. The one-dimensional Gaussian distributions  
 307 on the right show the fixation durations of the corresponding ROID. The table presents  
 308 the transition probabilities between the ROIDs. Note that the red and blue ROIDs are  
 309 spatially overlapping, but have different fixation durations.

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314 Figure 2. An acyclic graph representing the components, the parameters, and the  
 315 hyperparameters of an HMM. The colored nodes ( $o_n$ ) represent the observed fixation data;  
 316 the nodes on top ( $s_n$ ) represent the hidden states. The nodes on the left represent the prior  
 317 distributions of the HMM parameters;  $K$  represents the number of hidden states (ROIDs),  
 318 which is determined by the algorithm. The symbols left to the nodes represent the hyper-  
 319 parameters of the prior distributions.

320

321 For each participant, we trained two HMMs using either the eye movement data  
 322 from the learning phase (learning phase HMM) or the data from the recognition phase  
 323 (recognition phase HMM). We implemented the variational Bayesian expectation-  
 324 maximization (VBEM) algorithm (Bishop, 2006) in Matlab to estimate the parameters of  
 325 the HMMs. This Bayesian approach places a prior distribution on each parameter of the  
 326 model and then approximates the posterior distribution of the parameters using a  
 327 factorized variational distribution. The prior distributions for the Gaussian emissions  
 328 were Normal-Wishart distributions. For the spatial dimensions, we set the prior mean to  
 329 be the center of the image ( $m_0$  in Figure 2). The covariance matrices of the Gaussians  
 330 were set to be isotropic matrices with standard deviation of 14 pixels (0.53 degree of  
 331 visual angle) for the spatial dimensions ( $W_0$  in Figure 2), which was about the same size  
 332 as a facial feature on the image. For the temporal dimensions, we set the prior mean and

333 prior standard deviation using the fixation durations at the population level. The hyper-  
334 parameter  $v_0$  for the covariance matrices was set to 5, and the hyper-parameter  $\beta_0$  for the  
335 means was set to 1. The prior distributions for the transition matrix and prior vector were  
336 Dirichlet distributions, and we set the concentration parameter to 0.005 to reflect the  
337 assumption that the number of ROIDs on a face was much fewer than the number of  
338 fixation locations.

339 The VBEM algorithm for estimating an HMM proceeded as follows. First, we  
340 initialized the transition matrices ( $\varepsilon_0$  in Figure 2) and prior vectors ( $\alpha_0$  in Figure 2) as  
341 uniform distributions, and we obtained the initial Gaussian emissions (ROIDs) using the  
342 Matlab “fit” function for Gaussian mixture models. The VBEM algorithm then iterates  
343 between the E-step and the M-step until convergence. In the E-step, the forward-  
344 backward algorithm is used to calculate the single and pairwise responsibilities,  
345 corresponding to the marginal probability of a state at a particular time and the joint  
346 probability of two consecutive states, respectively. In the M-step, we updated the model  
347 parameters using the calculated responsibilities. All parameters of the HMMs were  
348 updated simultaneously during the E-M loop. To avoid convergence to a local maximum,  
349 we trained the model 100 times with different initial Gaussian ROIDs calculated by the  
350 Matlab fit function, and selected the model with the highest log-likelihood of the data.

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352 Finally, for each individual, we determined the number of hidden states (ROIDs) in  
353 their HMM in a data-driven fashion. In our previous study (Chuk et al., 2014), the  
354 number of hidden states for each model (HMM) was set to 3. In the current study, we  
355 implemented automatic model selection. We trained six separate HMMs with different  
356 numbers of ROIDs, ranging from 1 to 6. We then selected the HMM from this set with  
357 the highest log-likelihood of the data, thus determining the number of ROIDs for the  
358 individual. On our data, this selection method typically selected three or four hidden  
359 states. Note that we used a Bayesian methodology that automatically penalizes model  
360 complexity via the prior distributions on the model parameters. Hence, the selected model  
361 was the most parsimonious explanation of the data.

362

363 **Clustering Hidden Markov models**

364 In order to discover the common fixation patterns shared by participants, we  
365 clustered the individuals' HMMs into groups using the hierarchical variational  
366 expectation maximization (VHEM) algorithm (Coviello et al., 2012). For each group,  
367 VHEM generates a representative HMM that describes the ROIDs and transition  
368 probabilities for the common pattern used by the group. Furthermore, the log-likelihood  
369 of each participant's eye movement data was calculated with respect to each  
370 representative HMM, which yielded a measure of how similar their eye movement  
371 patterns were to the common patterns. For each participant and representative HMM, we  
372 calculated the average of the log-likelihoods of the fixation sequences over all trials. For  
373 each trial, the log-likelihood was normalized by dividing by the length of the sequence, in  
374 order to remove the effect of different sequence lengths (Oates, Firoui & Cohen, 2001;  
375 Seo, Kishino, & Thorne 2005; Martin, Hurn, & Harris, 2012). This measure was  
376 correlated with the participant's recognition performance in order to reveal whether  
377 certain common patterns were associated with better performance.

378 We applied the above clustering method separately for the learning phase and the  
379 recognition phase HMMs: the 48 learning phase HMMs were clustered into groups, and  
380 the 48 recognition phase HMMs were also clustered into groups. We clustered the  
381 participants' HMMs into two groups for each phase because several previous studies (e.g.,  
382 Blais et al., 2008; Kelly et al., 2011; Chuk, Chan, & Hsiao, 2014a) showed that most  
383 people's eye movement patterns exhibited one of the two fixation patterns: a holistic  
384 pattern that focused mainly at the center of the face, or an analytic pattern that focused at  
385 specific facial features (e.g., the two eyes and the mouth) in addition to the face center.  
386 Since we used a variational Bayesian approach to estimate parameters of individual  
387 HMMs, the input HMMs may have different numbers of hidden states. In the current  
388 modeling, the majority of the individual HMMs ended up having four ROIDs, and thus  
389 we set the representative HMMs in the VHEM algorithm to have four hidden states.

390 Previous studies (e.g. Hsiao & Cottrell, 2008) showed that participants had different  
391 eye movement patterns during the learning and the recognition phases, and that this  
392 difference was at least partly in terms of fixation duration. Therefore, we also tried to  
393 cluster the individuals' learning and recognition phase HMMs together into two clusters  
394 to see if participants indeed changed their eye movement strategies during the two phases

395 and whether the change was related to their recognition performance.

396

397

## 398 **Results**

### 399 **Eye movement patterns during the learning phase**

400 To discover common eye movement patterns participants used during the learning phase,

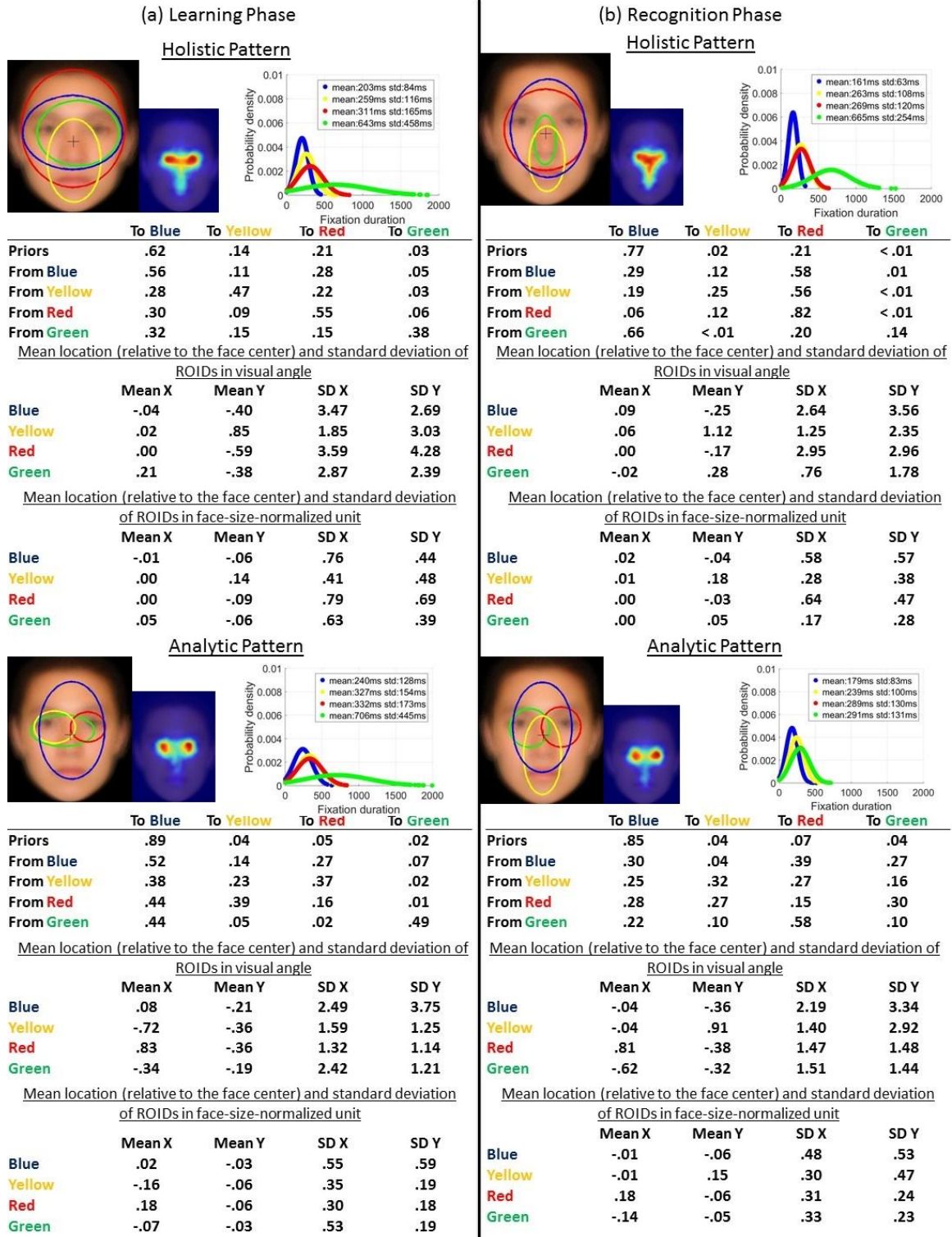
401 we modeled each participant's eye movements during the learning phase with an HMM

402 and clustered the individual HMMs into two groups. Figure 3a shows the representative

403 HMMs of the two resulting groups. Table 1 shows the number of participants being

404 clustered into each eye movement pattern group.

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Figure 3. The representative HMMs of the two common eye movement patterns discovered by clustering the HMMs for (a) the learning phase, and (b) the recognition phase. The figure shows the spatial distribution of the ROIDs and the corresponding heat



410 map, the duration distribution of the ROIDs (in ms), and the transition probability matrix  
 411 of the ROIDs. The tables below the transition matrix show the mean location (relative to  
 412 the face center) and standard deviation of the ROIDs in visual angle and in face-size-  
 413 normalized unit. Note that in (b), in the analytic pattern during the recognition phase, the  
 414 red and green ROIDs had very similar duration distributions, and thus the curves are  
 415 overlapped.

<b>Learning phase</b>			
<b>(a)</b>	Female	Male	<b>Total</b>
Holistic pattern	25	9	<b>34</b>
Analytic pattern	10	4	<b>14</b>
<b>(b)</b>	Caucasian	Asian	
Holistic pattern	16	18	<b>34</b>
Analytic pattern	8	6	<b>14</b>
<b>Recognition phase</b>			
<b>(a)</b>	Female	Male	<b>Total</b>
Holistic pattern	16	4	<b>20</b>
Analytic pattern	19	9	<b>28</b>
<b>(b)</b>	Caucasian	Asian	
Holistic pattern	11	9	<b>20</b>
Analytic pattern	13	15	<b>28</b>

416  
 417

418 Table 1. The number of participants being clustered into each eye movement pattern  
 419 group (analytic vs. holistic) with a breakdown by gender (a) and by race (b), using the  
 420 representative HMMs in Figure 3.

421

422 It can be seen that in the holistic representative HMM in Figure 3a, three of the four  
 423 ROIDs (except the yellow ROID) were centered at the bridge of the nose (i.e., the center  
 424 of the face). Participants in this group typically started a trial by looking at the center of  
 425 the face with a short fixation (M = 203 ms, blue ROID). Afterwards, they most likely  
 426 remained looking at the center with either a short fixation, (M = 203 ms) or a long  
 427 fixation (M = 311 ms, about 28% of the times, red ROID), and sometimes (11%) looked  
 428 at the tip of the nose/mouth region (duration M = 259 ms, yellow ROID). Occasionally  
 429 (about 5%) they made a very long fixation (M = 643 ms, green ROID) at the center of the  
 430 face. Since in this pattern, participants mainly looked at the center of the face, we refer to  
 431 this pattern as the holistic pattern during the learning phase.

432 In the analytic representative HMM shown in Figure 3a, the blue ROID was at the

433 center of the face, whereas a smaller, green ROID was slightly to the left of the center,  
 434 between the left eye and the bridge of the nose. The yellow and red ROIDs were located  
 435 at the left and right eye respectively. Participants in this group typically started a trial by  
 436 looking at the center of the face with a short fixation (M = 240 ms, blue ROID).  
 437 Afterwards, they either remained looking at the center of the face with short fixations  
 438 (blue ROID) or started looking at the two eyes (yellow and red ROIDs). When they  
 439 looked at the two eyes, the fixations were all with long duration (the left eye, M = 327 ms;  
 440 the right eye, M = 332 ms). Occasionally (6%), they looked between the left eye and the  
 441 bridge of the nose with a long fixation (M = 706 ms, green ROID). Since in this pattern,  
 442 participants looked at the two eyes specifically in addition to the face center, we refer to  
 443 this pattern as the analytic pattern during the learning phase.

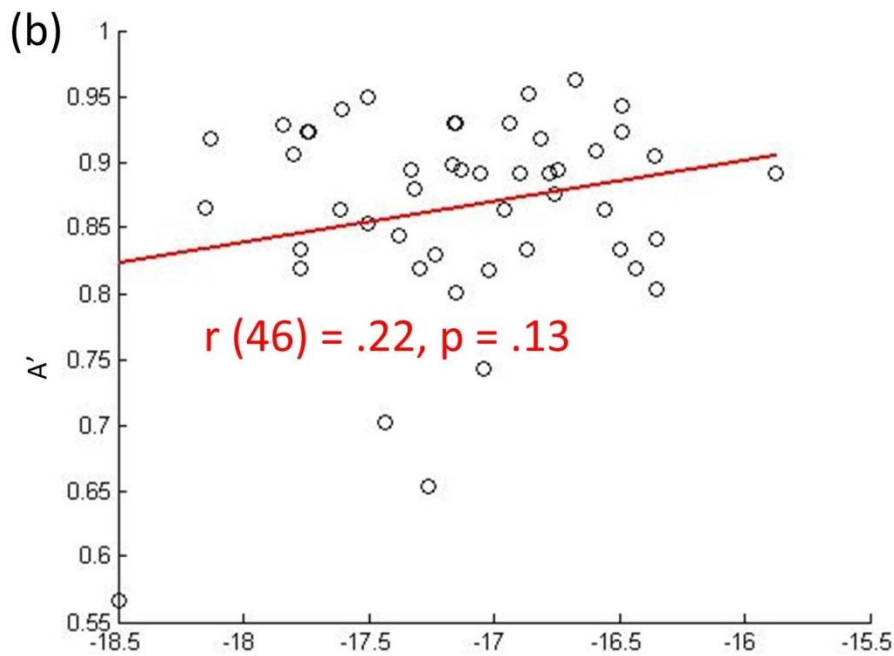
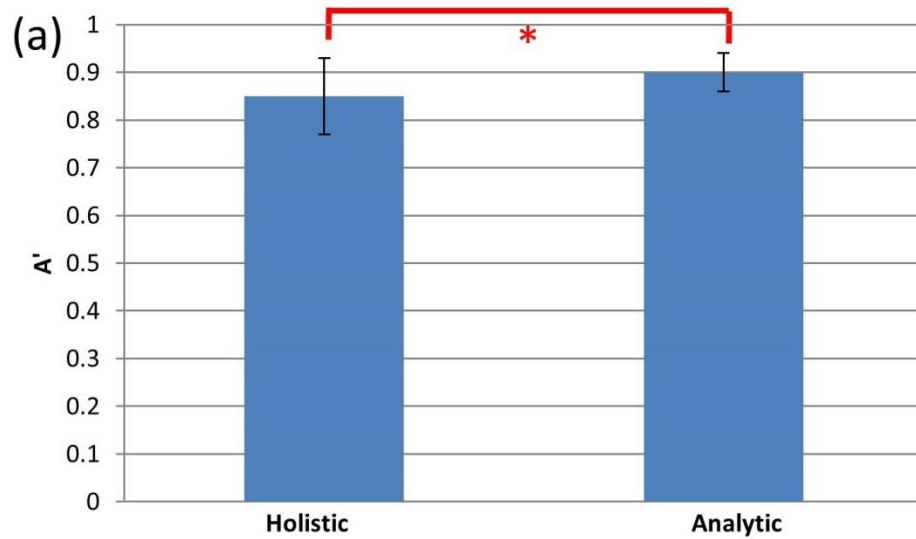
444 The two patterns showed a few similarities and differences. For both patterns, there  
 445 was an ROID with longer mean fixation duration (M > 600 ms) than the other ROIDs,  
 446 centered around the bridge of the nose (i.e., center of the face). However, the analytic  
 447 pattern had two ROIDs on the two eyes with relatively long fixation durations (M > 300  
 448 ms), which suggested that participants in this group looked specifically at the two eyes  
 449 with long fixation durations. In contrast, in the holistic pattern, the ROIDs were mostly at  
 450 the center of the face. These results suggested that people who showed holistic patterns  
 451 did not look at the eyes as much and as long as those who showed analytic patterns.  
 452 There were in total 34 participants who showed holistic patterns during the learning  
 453 phase; the other 14 participants showed analytic patterns. There were significantly more  
 454 participants showing holistic patterns than analytic patterns,  $\chi^2(1) = 8.33, p = .003$  (Table  
 455 1, learning phase).

456 We then compared the recognition performance of participants showing different eye  
 457 movement patterns during the learning phase using A-prime (A'). A-prime is a non-  
 458 parametric alternative to d-prime (d') and thus can be estimated when the hit or the false-  
 459 alarm rate was zero. The equations for A' are shown below.

$$A' = \begin{cases} .5 + \frac{(H - F)(1 + H - F)}{4H(1 - F)}, & \text{when } H \geq F \\ .5 - \frac{(F - H)(1 + F - H)}{4F(1 - H)}, & \text{when } H < F \end{cases}$$

460  
 461 where H represents the hit-rate, and F represents the false-alarm rate.

462           The results are shown in Figure 4a. We found that the participants showing analytic  
463 patterns ( $M = .90$ ) performed significantly better than those with holistic patterns ( $M$   
464  $= .85$ ),  $t(46) = 2.24$ ,  $p = .03$ . This result suggested that analytic patterns during face  
465 learning were beneficial for face recognition. We also computed the log-likelihoods of  
466 observing the 48 participants' learning phase eye movement data given the representative  
467 HMM of analytic patterns (Figure 3a) and examined whether they were correlated with  
468 participants' recognition performance. The log-likelihood measure reflected how similar  
469 a participant's eye movement pattern was to the representative analytic pattern. A higher  
470 value indicated higher similarity. The results (see Figure 4b), showed that although there  
471 was a positive correlation between the two measures, it did not reach significance,  $r(46)$   
472  $= .22$ ,  $p = .13$ . We further verified the finding with a skipped-correlation analysis, which  
473 identified outliers and estimated the correlation after the outliers were removed (Pernet,  
474 Wilcox, & Rousselet, 2013; the analysis discovered six outliers). The result was  
475 consistent with that reported above: the correlation between the two measures was not  
476 statistically significant,  $r(46) = .02$ . The log-likelihood of observing the participants'  
477 learning phase eye movement data given the representative HMM of holistic patterns also  
478 did not correlate with their recognition performance,  $r(46) = .13$ ,  $p = .37$ . These results  
479 suggested that although participants showing analytic patterns during face learning  
480 outperformed those showing holistic patterns in recognition, the similarities of their eye  
481 movement patterns to the representative analytic/holistic pattern were not good predictors  
482 for their recognition performance.  
483



**Log-likelihood of eye movement patterns being classified as analytic**

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Figure 4. (a) Recognition performance of participants with different eye movement patterns during the learning phase, measured in A'. (b) The correlation between the log-likelihoods of the participants' eye movement patterns being classified as analytic and their recognition performances in A'.

Was the advantage of participants with analytic patterns in recognition performance

492 related to the number of fixations they made during the learning phase? We found that  
493 participants with holistic patterns ( $M = 14.46$ ) made a similar number of fixations to  
494 those with analytic patterns ( $M = 13.17$ ),  $t(46) = 1.72$ ,  $p = .09$ . This result suggested that  
495 the advantage of analytic patterns was not due to a larger number of fixations made.  
496 Instead, it may be the active sampling of information from the two eyes, the most  
497 diagnostic features for face recognition, during face learning/encoding.

498

### 499 **Eye movement patterns during the recognition phase**

500 To discover common eye movement patterns participants used during the recognition  
501 phase, we modeled each participant's eye movements during the recognition phase with  
502 an HMM and clustered the individual HMMs into two groups. The representative HMMs  
503 of the two groups are shown in Figure 3b.

504 It can be seen from Figure 3b that the four ROIDs of the holistic representative  
505 HMM were all around the center of the face. The red and blue ROIDs covered the central  
506 region of the face. The yellow ROID was at the lower part of the face, covering the tip of  
507 the nose and the mouth. The green ROID covered the nose. Participants in this group  
508 typically began a trial by looking at the center of the face with a short fixation ( $M = 161$   
509 ms, blue ROID). Then they looked at the center of the face with either long ( $M = 269$  ms,  
510 red ROID) or short fixation duration ( $M = 161$  ms, blue ROID), or occasionally (12%)  
511 they looked at the tip of the nose. Only in very rare cases (1%) would they look at the  
512 center of the nose with very long duration ( $M = 665$  ms, green ROID). This pattern  
513 focused mainly at the center of the face, and thus we identified it as the holistic eye  
514 movement pattern.

515 The analytic representative HMM shown in Figure 3b had two ROIDs (the green  
516 and the red ROIDs) on the two eyes respectively. In addition, the blue ROID was at the  
517 center of the face, whereas the yellow ROID was at the tip of the nose and covered the  
518 nose and the mouth region. Participants in this group were most likely to begin a trial by  
519 looking at the center of the face with a short fixation ( $M = 179$  ms, blue ROID). Then,  
520 they either remained looking at the center (30% of the times), or looked at the left eye  
521 (27%) or the right eye (39%) with a slightly longer fixation (left eye:  $M = 291$  ms; right  
522 eye:  $M = 289$  ms). They rarely (4%) looked at the nose and the mouth. When they

523 looked at one of the eyes, their next fixation was most likely to be at the other eye,  
524 suggesting that participants in this group preferred to switch their attention between the  
525 eyes. Since this pattern showed focuses on the eyes in addition to the face center, we  
526 identified it as the analytic eye movement pattern.

527 The two patterns had some similarities and differences. In both patterns, participants  
528 were most likely to start a trial with a brief fixation at around the center of the face,  
529 followed by fixations with duration around 250 to 300 ms. Nevertheless, in the holistic  
530 pattern, these subsequent fixations were mostly located around the center of the face,  
531 whereas in the analytic pattern, these subsequent fixations were specifically at the two  
532 eyes. There were in total 20 participants who showed holistic patterns during the  
533 recognition phase, and 28 participants showed analytic patterns. The percentages of the  
534 participants using the two patterns did not differ significantly from each other,  $\chi^2(1) =$   
535 1.33,  $p = .25$  (Table 1, recognition phase). When we compared the distribution of the  
536 participants over the two patterns during recognition with that during learning, there were  
537 significantly more participants adopting holistic patterns during learning than recognition,  
538  $\chi^2(1) = 8.30, p = .004$ .

539 When we compared these patterns with those observed during the learning phase,  
540 we found that the representative holistic patterns of the two phases were significantly  
541 different. The log-likelihoods of observing the holistic eye movement data during the  
542 learning phase given the representative holistic HMM of the learning phase and the log-  
543 likelihoods of observing the same data given the representative holistic HMM of the  
544 recognition phase were significantly different,  $t(33) = 4.47, p < .001$ . The log-likelihoods  
545 of observing the holistic eye movement data during the recognition phase given the two  
546 representative holistic HMMs were also significantly different,  $t(19) = 4.56, p < .001$ .  
547 The difference between the two log-likelihoods was an approximation to the Kullback-  
548 Leibler (KL) divergence between the learning phase and recognition phase representative  
549 holistic HMMs, which was a measure of difference between two distributions (Chuk et  
550 al., 2014). Similarly, the representative analytic patterns of the two phases were  
551 significantly different. The log-likelihoods of observing the analytic eye movement data  
552 during the learning phase given the two representative analytic HMMs were significantly  
553 different,  $t(13) = 2.12, p = .05$ ; similarly for those observed during the recognition phase,

554  $t(27) = 4.43, p < .001$ . When we compared the number of fixations per trial that  
555 participants made during the two phases, we found that participants made significantly  
556 more fixations during the learning phase regardless of whether they used holistic patterns  
557 ( $M = 14.46$  for learning phase,  $M = 6.49$  for recognition phase,  $t(52) = 12.55, p < .001$ ) or  
558 analytic patterns ( $M = 13.17$  for learning phase,  $M = 5.85$  for recognition phase,  $t(40) =$   
559  $10.61, p < .001$ ). We also found that the average fixation durations were significantly  
560 longer during the learning phase than the recognition phase regardless of whether  
561 participants used holistic patterns ( $M = 336.26$  ms for learning phase,  $M = 246.94$  ms for  
562 recognition phase,  $t(40) = 4.79, p < .001$ ) or analytic patterns ( $M = 297.97$  ms for  
563 learning phase,  $M = 244.27$  ms for recognition phase,  $t(52) = 2.91, p = .005$ ).

564 We also compared the durations of the fixations within the ROIDs between the two  
565 phases. The durations of the fixations at around the face center in the holistic pattern  
566 during face learning (Figure 3a, blue and red ROIDs,  $M = 203$  ms and  $311$  ms  
567 respectively) were slightly longer than those observed in the holistic pattern during face  
568 recognition (Figure 3b, blue and red ROIDs,  $M = 161$  ms and  $269$  ms respectively;  $t(6543)$   
569  $= 19.37, p < 0.001$ , and  $t(7067) = 11.56^1, p < .001$ , respectively). Similarly, the durations  
570 of the fixations at the two eyes in the analytic pattern during face learning (Figure 3a,  
571 yellow and red ROIDs,  $M = 327$  ms and  $332$  ms respectively) were slightly longer than  
572 those observed in the analytic pattern during face recognition (Figure 3b, green and red  
573 ROIDs,  $M = 291$  and  $289$  ms respectively;  $t(4044) = 7.85, p < .001$ , and  $t(4185) = 9.09, p$   
574  $< .001$ , respectively).

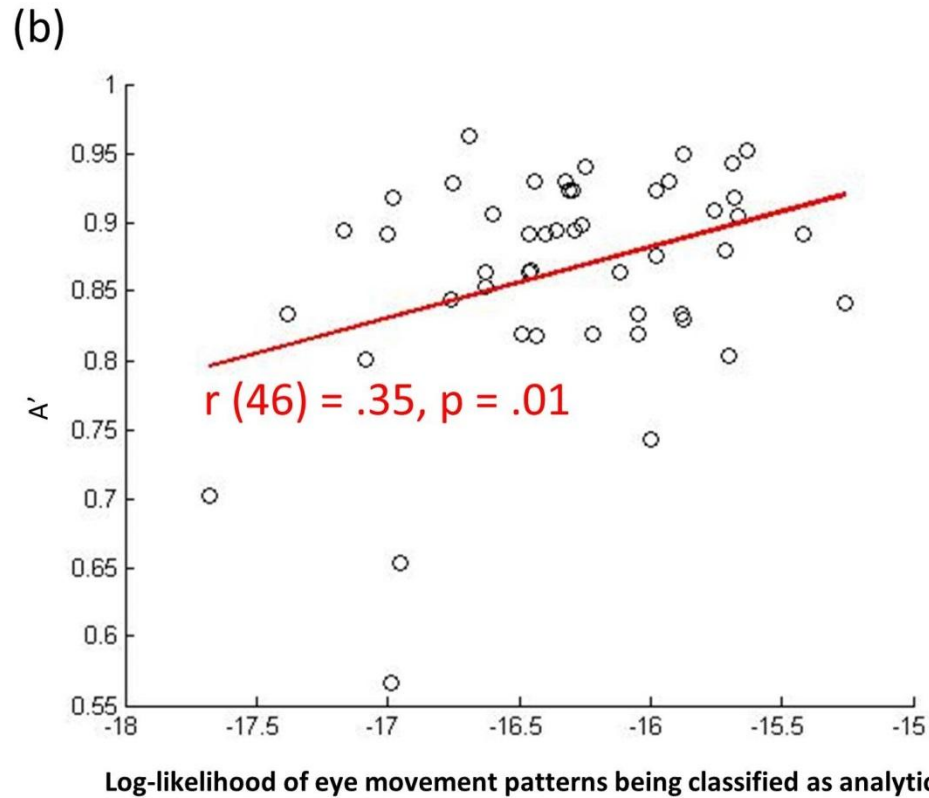
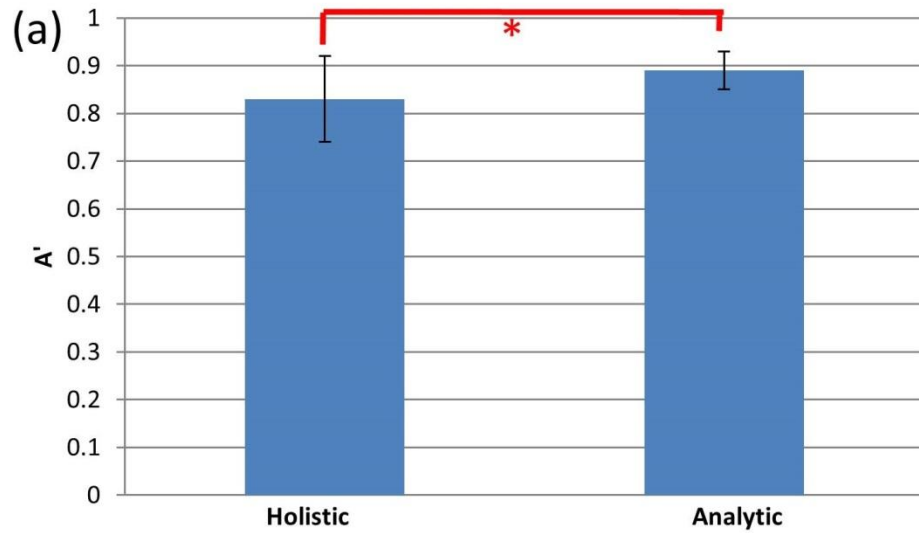
575 Regarding participants' recognition performance, we found that participants with  
576 analytic patterns ( $M = .89$ ) performed significantly better than those using holistic  
577 patterns ( $M = .83$ ),  $t(46) = 3.13, p = .003$  (Figure 5a). In addition, the log-likelihoods of  
578 observing participants' recognition phase eye movements given the representative HMM  
579 of analytic patterns was positively correlated with participants' recognition performances  
580 in A',  $r(46) = .35, p = .01$  (Figure 5b). We further verified the finding with a skipped-  
581 correlation analysis. The result was consistent with that reported above; no outlier was  
582 identified. In contrast, this correlation was not significant using the representative HMM

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<sup>1</sup> We estimated the numbers of fixations that were responsible for the two ROIDs and used them as the sample sizes for the t-tests. The means and standard deviations are shown in the corresponding figures. The comparison of the ROIDs was done using unpaired t-tests.

583 of holistic patterns,  $r(46) = .15$ ,  $p = .30$ . These results were consistent with our previous  
584 study (Chuk et al., 2014b; Chuk et al., submitted), suggesting that analytic eye movement  
585 patterns were beneficial for face recognition. In addition, participants using the two  
586 patterns did not differ significantly in the number of fixations made per trial,  $t(46) = 1.22$ ,  
587  $p = .23$  (holistic patterns,  $M = 6.63$ ; analytic patterns,  $M = 5.91$ ) or response time (holistic  
588 patterns,  $M = 1.95$  s; analytic patterns,  $M = 1.76$  s),  $t(46) = 1.54$ ,  $p = .13$ . This result  
589 suggested that the advantage of analytic patterns over holistic patterns was not simply  
590 because participants with analytic patterns made more fixations on the face.  
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593

594 Figure 5. (a) Recognition performance of participants with different eye movement

595 patterns during the recognition phase, measured in A'. (b) The correlation between the

596 log-likelihoods of participants' eye movement patterns being classified as analytic and

597 their recognition performances.

598

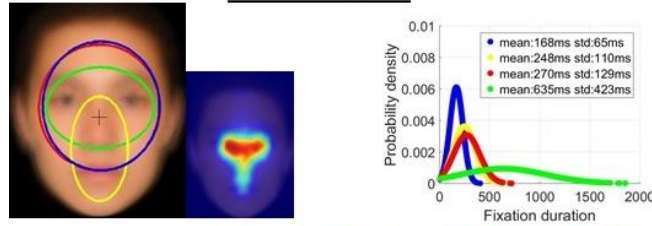
599 **Did participants use the same eye movement patterns for the learning and**  
600 **recognition phases?**

601 In the previous sections, we found that during the learning phase, a majority of  
602 participants used holistic eye movement patterns. In contrast, during the recognition  
603 phase, there were similar percentages of participant using analytic and holistic patterns.  
604 This result suggests participants might have used different eye movement patterns during  
605 the two phases. To test this, we clustered participants' learning and recognition phase  
606 HMMs into two groups to discover common patterns among them, and examined  
607 whether a majority of participants used the same patterns for face learning and  
608 recognition. The resulting patterns are shown in Figure 6. Table 2 shows the number of  
609 participants being clustered into each eye movement pattern group.

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Holistic Pattern



	To Blue	To Yellow	To Red	To Green
Priors	.47	.08	.43	.02
From Blue	.30	.11	.56	.03
From Yellow	.11	.34	.52	.03
From Red	.03	.09	.79	.09
From Green	.02	.06	.58	.34

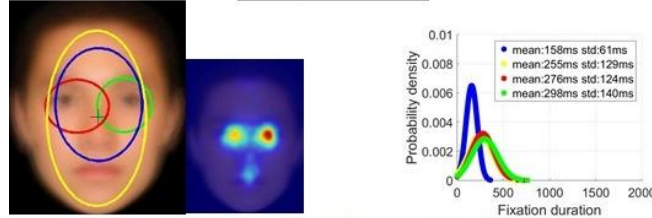
Mean location (relative to the face center) and standard deviation of ROIDs in visual angle

	Mean X	Mean Y	SD X	SD Y
Blue	.06	-.36	3.06	3.34
Yellow	.02	1.00	1.51	2.73
Red	.02	-.32	3.17	3.26
Green	.04	-.30	2.83	2.12

Mean location (relative to the face center) and standard deviation of ROIDs in face-size-normalized unit

	Mean X	Mean Y	SD X	SD Y
Blue	.01	-.06	.68	.53
Yellow	.00	.16	.33	.44
Red	.00	-.05	.69	.52
Green	.01	-.05	.63	.34

Analytic Pattern



	To Blue	To Yellow	To Red	To Green
Priors	.66	.23	.05	.06
From Blue	.22	.15	.27	.36
From Yellow	.11	.55	.14	.20
From Red	.05	.29	.12	.54
From Green	.10	.41	.37	.12

Mean location (relative to the face center) and standard deviation of ROIDs in visual angle

	Mean X	Mean Y	SD X	SD Y
Blue	.02	-.40	2.27	2.96
Yellow	-.04	.04	2.61	4.62
Red	-.66	-.34	1.66	1.40
Green	.85	-.38	1.40	1.40

Mean location (relative to the face center) and standard deviation of ROIDs in face-size-normalized unit

	Mean X	Mean Y	SD X	SD Y
Blue	.00	-.06	.50	.47
Yellow	-.01	.01	.56	.74
Red	-.14	-.05	.36	.23
Green	.19	-.06	.31	.23

661 Figure 6. The representative HMMs of the two common eye movement patterns  
 662 discovered by clustering all participants' HMMs (including both learning and recognition  
 663 phases) together. The figure shows the spatial distribution of the ROIDs and the  
 664 corresponding heat map, the duration distribution of the ROIDs, and the transition  
 665 probability matrix of the ROIDs. The tables below the transition matrix show the mean  
 666 location (relative to the face center) and standard deviation of the ROIDs in visual angle  
 667 and in face-size-normalized unit.

<b>Learning phase</b>			
<b>(a)</b>	Female	Male	<b>Total</b>
Holistic pattern	26	9	<b>35</b>
Analytic pattern	9	4	<b>13</b>
<b>(b)</b>	Caucasian	Asian	
Holistic pattern	18	17	<b>35</b>
Analytic pattern	6	7	<b>13</b>
<b>Recognition phase</b>			
<b>(a)</b>	Female	Male	<b>Total</b>
Holistic pattern	16	4	<b>20</b>
Analytic pattern	19	9	<b>28</b>
<b>(b)</b>	Caucasian	Asian	
Holistic pattern	12	8	<b>20</b>
Analytic pattern	12	16	<b>28</b>

669  
 670 Table 2. The number of participants being clustered into each eye movement pattern  
 671 group (analytic vs. holistic) with a breakdown by gender (a) and by race (b), using the  
 672 representative HMMs in Figure 6.

673  
 674 It can be seen that in the holistic representative HMM in Figure 6, the red, blue, and  
 675 green ROIDs centered at the bridge of the nose, and the yellow ROID covered the nose  
 676 and the mouth region. In this pattern, participants were most likely to begin a trial with a  
 677 longer ( $M = 270$  ms) or a shorter ( $M = 168$  ms) fixation at the center of the face.  
 678 Afterwards, they typically made a long ( $M = 270$  ms) fixation at around the center of the  
 679 face. Occasionally, they looked at the center of the face with much longer durations ( $M =$   
 680 635 ms, green ROID), or the tip of the nose/mouth region (yellow ROID). This pattern  
 681 reflected a focus at the center of the face, and thus we identified it as the holistic eye  
 682 movement pattern.

683 The analytic representative HMM shown in Figure 6 reflected a different eye

684 movement pattern. The blue and the yellow ROIDs both centered at the bridge of the  
 685 nose, whereas the red and the green ROIDs were located at the left and the right eye  
 686 respectively. In this pattern, participants were most likely to begin a trial with a short  
 687 fixation at the center of the face ( $M = 158$  ms, blue ROID), followed by a longer fixation  
 688 on either the right eye ( $M = 298$  ms) or the left eye ( $M = 276$  ms). Sometimes they  
 689 remained looking at the center with either a short ( $M = 158$  ms, blue ROID) or a longer  
 690 ( $M = 255$  ms, yellow ROID) fixation. Since this pattern showed specific focuses on the  
 691 two eyes in addition to the face center, we identified it as the analytic eye movement  
 692 pattern.

693 We found that 35 participants' learning phase HMMs were clustered into the holistic  
 694 pattern and 13 were clustered into the analytic pattern. For the recognition phase HMMs,  
 695 20 participants' HMMs were clustered into the holistic pattern and 28 were clustered into  
 696 the analytic pattern (Table 2). As summarized in Table 3 below, 19 (about 40%)  
 697 participants used different eye movement patterns between the two phases, and 29  
 698 participants used the same patterns between the two phases. The percentages of  
 699 participants using the same or different patterns between the two phases did not differ  
 700 significantly,  $\chi^2(1) = 2.08$ ,  $p = .15$ . Interestingly, among participants who used different  
 701 patterns during the two phases, 90% of them (17/19) switched their patterns from holistic  
 702 at learning to analytic at recognition.

703

<b>Pattern switch</b>		<i>recognition phase</i>		
		same	different	<b>Total</b>
<i>learning</i>	holistic	18	17	<b>35</b>
<i>phase</i>	analytic	11	2	<b>13</b>
<b>Total</b>		<b>29</b>	<b>19</b>	<b>48</b>

704

705 Table 3. Number of participants switched patterns during the two phases.

706

707 To test whether participants' perceptuomotor memory during face learning played  
 708 an important role in their recognition performance, as suggested by the scan path theory,  
 709 we examined whether participants who used the same eye movement patterns between  
 710 face learning and recognition outperformed those who used different patterns in face

711 recognition. The results showed that the two groups did not differ significantly in  
712 recognition performance (participants who used different patterns,  $M = .87$ ; participants  
713 who used same patterns,  $M = .86$ ),  $t(46) = .36$ ,  $p = .72$ . In a separate analysis, we  
714 performed a  $2 \times 2$  ANOVA with learning phase eye movement pattern (holistic vs.  
715 analytic) and recognition phase eye movement pattern (holistic vs. analytic) as  
716 independent variables and recognition performance in A' as the dependent variable. We  
717 found that the two factors did not interact with each other,  $F(1, 44) = .06$ ,  $p = .82$ ,  
718 suggesting that whether participants changed their eye movement patterns between the  
719 learning and the recognition phases did not significantly modulate recognition  
720 performance. Note however that this analysis was based on unequal numbers of  
721 participants in each condition, as shown in Table 3. We also examined whether  
722 participants' recognition performance was correlated with the similarity between their  
723 learning phase and recognition phase eye movement patterns. To do this, for each  
724 participant, we calculated the log-likelihoods of observing the participant's recognition  
725 phase eye movement data given his/her learning phase and recognition phase HMMs. The  
726 difference between the two log-likelihoods represented the KL-divergence between the  
727 learning phase and recognition phase HMMs, a measure of similarity between the two  
728 eye movement patterns. We found that this similarity measure did not correlate with  
729 recognition performance,  $r(46) = .18$ ,  $p = .22$ . Similarly, the correlation using the  
730 participants' learning phase eye movement data was not significant,  $r(46) = .11$ ,  $p = .44$ .  
731 These results suggested that the similarity between learning phase and recognition phase  
732 eye movement patterns did not predict recognition performance.

733

## 734 **Discussion**

735 In this study, we aimed to examine the relationship between eye movement patterns  
736 during face learning and recognition, and its association with recognition performance in  
737 a face recognition memory task. To reflect individual differences in both spatial and  
738 temporal dimensions of eye movements in our data analysis, we used a hidden Markov  
739 model (HMM) based approach (Chuk et al., 2014), in which each participant's eye  
740 movement pattern was modeled with an HMM. The hidden states of the HMMs  
741 represented regions of interest and duration (i.e., ROID) of participants' fixations. The

742 eye movements among these ROIDs were summarized with a transition matrix in the  
743 model. This information was estimated from participants' eye movement data in a  
744 completely data-driven fashion. Individual HMMs then could be clustered according to  
745 their similarities to discover common patterns shared by individuals. The similarity  
746 between an individual's eye movement pattern to a common pattern discovered through  
747 clustering could be calculated as the likelihood of the individual pattern being classified  
748 as the common pattern. This similarity measure then could be used to examine the  
749 association between eye movement patterns and recognition performance. Note that in  
750 contrast to the HMMs used in our previous studies (e.g., Chuk et al., 2014), the HMM  
751 used in the current study was improved in two aspects. First, the number of hidden states  
752 was determined through model selection instead of pre-specified. Second, we included  
753 fixation duration information in addition to fixation location information. This is to  
754 reflect the previous finding that eye movements during face learning and recognition  
755 differed in fixation duration (Hsiao & Cottrell, 2008). The new model thus was able to  
756 more accurately summarize a participant's eye movement behavior in a cognitive task.

757 Our results showed that both holistic (i.e., looking mainly at the face center) and  
758 analytic eye movement patterns (i.e., looking specifically at the two eyes in addition to  
759 the face center) could be observed during face learning and recognition. Nevertheless, the  
760 holistic and analytic patterns observed during face learning differed significantly from  
761 those observed during face recognition. Eye movements during the learning phase  
762 occasionally involved long fixations at around the center of the face, which was rarely the  
763 case during the recognition phase. In addition, the fixations during learning were in  
764 general longer and more numerous than those observed during recognition. Interestingly,  
765 we found that significantly more participants adopted holistic patterns during face  
766 learning than recognition. Combined, these results suggested that in general participants  
767 showed different eye movement patterns between face learning and recognition,  
768 demonstrating different cognitive processes involved for information encoding and  
769 retrieval.

770 Hsiao and Cottrell (2008) observed that when comparing the first three fixations  
771 during the learning and recognition phases, during learning participants' fixation duration  
772 gradually increased from the first to the third fixations, whereas during the recognition

773 phase, the first three fixations were of similar durations. This pattern was in general  
774 consistent with our results. During face learning, most participants adopted holistic  
775 patterns. In the representative holistic pattern during learning (Figure 3a), participants  
776 typically started a trial with a short fixation at the face center (M = 203 ms, blue ROID),  
777 and gradually transited to longer fixations at the face center at third fixation (M = 311 ms,  
778 red ROID). Whereas during face recognition, in both holistic and analytic patterns,  
779 participants typically started with a short fixation (M ~ 170 ms), followed by slightly  
780 longer fixations (M ~ 278 ms) at both the second and third fixations. In contrast to our  
781 finding, Blais et al. (2008) and Caldara et al. (2010) found that participants' fixation  
782 durations did not differ between the learning and recognition phases using group-level  
783 analysis. We speculate that this discrepancy may be due to substantial individual  
784 differences in eye movement pattern during the two phases. Our approach allowed us to  
785 discover different patterns within each phase, and compare corresponding ROIDs in  
786 similar patterns across the two phases. And thus we were able to better discover this  
787 difference in fixation duration between the two phases.

788         Although the holistic and analytic eye movement patterns during the learning and  
789 recognition phases differed in fixation duration, we found that in both phases, participants  
790 with analytic patterns outperformed those with holistic patterns in recognition  
791 performance. This finding was consistent with Sekiguchi's (2011) finding that  
792 participants who performed better in face recognition moved their eyes between the left  
793 and right eyes more often during face learning as compared with those who performed  
794 worse. Note that this advantage of analytic patterns was not because participants using  
795 analytic patterns made more fixations per trial than those using holistic patterns, as the  
796 two groups of participants did not differ significantly in number of fixations made per  
797 trial either for face learning or recognition. Instead, this advantage of analytic patterns  
798 was likely to be due to active information encoding and retrieval from the two eyes,  
799 suggesting that information about the two eyes is important for face recognition.  
800 Consistent with this finding, the two eyes have been reported to be the most diagnostic  
801 features participants used for face recognition (e.g., Gosselin & Schyns, 2001; Vinette et  
802 al., 2004). The eyes also have been proposed to provide important signals for the  
803 direction of social attention (e.g., Langton, Watt, & Bruce, 2000). In addition, as



804 compared with whole faces, eyes presented in isolation are shown to elicit larger N170  
805 ERP amplitude, an electrophysiological marker proposed to reflect the neural mechanism  
806 for face detection, suggesting the importance of eyes in face perception (Bentin, Allison,  
807 Puce, Perez, & McCarthy, 1996; see also Taylor, Itier, Allison, & Edmonds, 2001; Taylor,  
808 Edmonds, McCarthy, & Allison, 2001). Although analytic eye movement patterns during  
809 both face learning and recognition seemed to be beneficial for face recognition, we found  
810 that participants' recognition performance was positively correlated with the log-  
811 likelihood of participants' eye movements being classified as analytic during the  
812 recognition phase, but not with that during the learning phase. This finding suggested that  
813 eye movement patterns during the recognition phase may be a better predictor for  
814 participants' recognition performance than those during the learning phase.

815 Miellet, Caldara, and Schyns (2011) showed that during face recognition,  
816 participants' eye fixations on the eyes of the face images were associated with perception  
817 of local information, whereas those at the center of the face were associated with  
818 perception of global information. According to this finding, participants using the  
819 analytic and holistic eye movement patterns identified in the current study may engage  
820 different types of information processing in face recognition. More specifically,  
821 participants with holistic patterns (i.e., looking mainly at the face center) may have  
822 primarily engaged in global/configural face processing, whereas those with analytic  
823 patterns (i.e., focusing on the individual eyes in addition to the face center) may have  
824 engaged in both global and local/featural face processing. While global/configural  
825 information was reported to play an important role in face recognition (e.g. Bartlett &  
826 Searcy, 1993; Leder & Bruce, 1998), most recent studies have suggested that both  
827 local/featural and global/configural information are important for recognizing faces (e.g.,  
828 Burton, Schweinberger, Jenkins, & Kaufmann, 2015; Cabeza & Kato, 2000; Sandford &  
829 Burton, 2014). Consistent with this finding, in automatic face recognition in computer  
830 vision, the best performing algorithms made use of both local and global representations  
831 of the faces (Bonnen, Klare, & Jain, 2013; Ding, Shu, Fang, & Ding, 2010). Together,  
832 these findings suggested that active retrieval of both global and local face representations  
833 through analytic eye movement patterns may be optimal for face recognition.

834 In order to examine whether individual participants used the same or different eye

835 movement patterns between the learning and the recognition phases, in a separate  
836 analysis we clustered participants' learning and recognition phase HMMs together into  
837 two groups to discover common patterns shared between the two phases. The resulting  
838 two representative HMMs (Figure 6) showed similar characteristics as the holistic and  
839 analytic patterns discovered when we clustered participants' patterns in the learning and  
840 recognition phases separately. We then examined whether individual participants used the  
841 same or different patterns between the learning and recognition phases. We found that  
842 about 40% of the participants used different eye movement patterns between the learning  
843 and recognition phases, and the percentages of the participants using the same or different  
844 patterns did not differ significantly from each other. Interestingly, among those who used  
845 different patterns between learning and recognition, 90% of them switched from holistic  
846 at learning to analytic at recognition, suggesting that analytic patterns were preferred  
847 during recognition. These results showed that participants do not necessarily use the same  
848 eye movement patterns for face learning and recognition, This finding was in contrast to  
849 previous studies that observed similar eye movement patterns between the learning and  
850 recognition phases using group-level eye movement data analysis (e.g., Blais et al., 2008;  
851 Caldara et al., 2010). This individual difference in the similarity of eye movements  
852 between learning and recognition may have been obscured in the group-level data  
853 analysis. This phenomenon demonstrated well the advantage of our approach for data  
854 analysis at the individual level.

855         According to the scan path theory (Noton & Stark, 1971a; 1971b), recapitulation  
856 of the eye movement/perceptuomotor pattern produced during learning is necessary for  
857 recognition to be successful. If perceptuomotor memory elicited by eye movements does  
858 play an important role for recognition performance, we would expect that participants  
859 who used the same eye movement pattern between the learning and recognition phases  
860 outperformed those who used different eye movement patterns in the recognition task.  
861 Nevertheless, the results of our analysis did not support this hypothesis. We found that  
862 participants who showed the same or different eye movement patterns between the two  
863 phases did not differ significantly in their recognition performance. In addition, the  
864 similarity between their eye movement patterns during the learning and the recognition  
865 phases did not significantly correlate with their recognition performance. Instead, we

866 found that analytic eye movement patterns during the recognition phase, which focused  
867 on the two eyes in addition to the face center, seemed to be the best predictor for  
868 participants' recognition performance. This phenomenon suggested that retrieval of the  
869 most diagnostic features for recognition is more important than recapitulation of the  
870 perceptuomotor cycles/eye movements produced during learning in visual recognition. To  
871 confirm the speculation that eye fixations at more diagnostic features for recognition lead  
872 to better recognition performance, future work will directly manipulate participants' eye  
873 movement patterns (such as through cueing or training paradigms; e.g., Hills & Lewis,  
874 2011) and examine whether it modulates their recognition performance.

875 Note that in the current study, we used the same images for old faces during the  
876 learning and recognition phases, following a majority of face recognition studies in the  
877 literature (e.g., Barton et al., 2006; Hayward, Rhodes, & Schwaninger, 2008; Henderson,  
878 Williams, & Falk, 2005; Hsiao & Cottrell, 2008). However, real-life face recognition  
879 typically involves recognizing faces under different conditions, such as different  
880 orientations, expressions, or lighting conditions. Future work will examine how these  
881 different task demands modulate the association between participants' eye movement  
882 patterns and performance in face recognition.

883 In summary, through analyzing eye movement data at the individual level using  
884 the HMM based approach, here we showed that both holistic and analytic eye movement  
885 patterns could be observed during face learning and recognition. Eye movements during  
886 learning generally involved longer fixation duration than those during recognition.  
887 During both face learning and recognition, participants who showed analytic patterns  
888 performed better than those with holistic patterns in the recognition task, although a  
889 significant correlation between eye movement patterns and recognition performance was  
890 only observed for eye movements during the recognition phase. This finding suggested  
891 that the retrieval of diagnostic features for recognition, such as the eyes, is a good  
892 predictor for performance in face recognition. In contrast to the scan path theory, which  
893 posits eye movements produced during learning have to be repeated during recognition  
894 for the recognition to be successful, we found that participants used the same eye  
895 movement pattern for face learning and recognition did not differ from those used  
896 different patterns in recognition performance. In addition, the similarity between the eye

897 movement patterns during face learning and recognition did not correlate with  
898 recognition performance. These results suggested that perceptuomotor memory elicited  
899 by eye movement patterns during learning does not play an important role in recognition.  
900 In contrast, it is the retrieval of diagnostic information during recognition that is essential  
901 for recognition to be successful. This finding has very important implications for ways to  
902 improve recognition performance in both healthy and clinical populations.

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905

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912

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